

What do I need to be able to do?

By the end of this unit you should be able to:

- Understand and use factors
- Understand and use multiples
- Multiply/ Divide integers and decimals by powers of 10
- Use formal methods to multiply
- Use formal methods to divide
- Understand and use order of operations
- Solve area problems
- Solve problems using the mean

Keywords**Array:** an arrangement of items to represent concepts in rows or columns**Multiples:** found by multiplying any number by positive integers**Factor:** integers that multiply together to get another number.**Mil:** prefix meaning one thousandth**Centi:** prefix meaning one hundredth**Kilo:** prefix meaning multiply by 1000**Quotient:** the result of a division**Dividend:** the number being divided**Divisor:** the number we divide byFactors

Arrays can help represent factors

Factors of 10 1, 2, 5, 10

10 x 1 or 1 x 10

5 x 2 or 2 x 5

The number itself is always a factor

Square numbers have an **ODD** number of factors**Factors of 4**

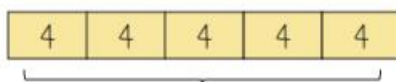
1, 2, 4

Factors of 36

1, 2, 3, 4, 6, 9, 12, 18, 36

Be strategic

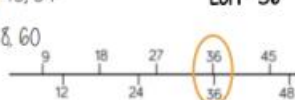
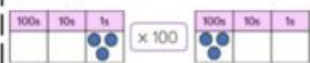
- Lay factors out in pairs can help you not to miss any

Multiples

Bar models can represent by something is a multiple. Eg. 20 is a multiple of 4

Lowest Common Multiples**9** 9, 18, 27, 36, 45, 54**12** 12, 24, 36, 48, 60**LCM of 9 and 12**

The first time their multiples match

LCM = 36Multiply/ Divide by powers of 10

$$3 \times 100 = 300$$



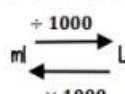
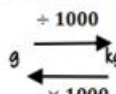
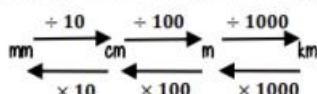
$$0.03 \times 100 = 3$$

Repeated multiplication and division by powers of 10 is commutative

$$\div 10 \text{ then } \div 10 \longrightarrow \div 100$$

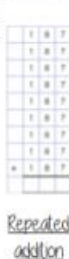
Metric conversions

Useful Conversions:

Multiplication methods

Long multiplication (column)

Grid method



Repeated addition

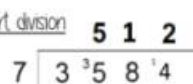
Less effective method especially for bigger multiplication

Multiplication with decimalsPerform multiplications as integers
eg. $0.2 \times 0.3 \longrightarrow 2 \times 3$ Make adjustments to your answer to match the question: $0.2 \times 10 = 2$

$$0.3 \times 10 = 3$$

Therefore $6 \div 100 = 0.06$ **Estimations:** Using estimations allows a 'check' if your answer is reasonableDivision methods

$$3584 \div 7 = 512$$

Short division**Complex division**

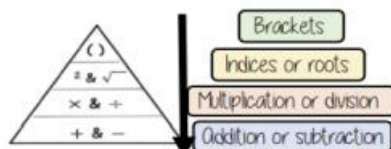
$$\div 24 = \div 6 \div 4$$

Break up the divisor using factors

Division with decimals

The placeholder in division methods is essential – the decimal lines up on the dividend and the quotient

$$24 \div 0.02 \longrightarrow 24 \div 0.2 \longrightarrow 240 \div 2$$

All give the same solution as represent the same proportion
Multiply the values in proportion until the divisor becomes an integerOrder of operations

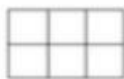
If you have multiple operations from the same tier work from left to right

$$\text{eg } 10 - 3 + 5 \longrightarrow 10 - 3 \longrightarrow 7 + 5$$

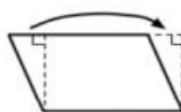
$$6 \times 4 + 8 \times 2 = 24 + 16 = 40$$

Area problems**Rectangle**

Base x Perpendicular height

**Parallelogram/ Rhombus**

Base x Perpendicular height

**Triangle** $\frac{1}{2} \times \text{Base} \times \text{Perpendicular height}$

A triangle is half the size of the rectangle it would fit in

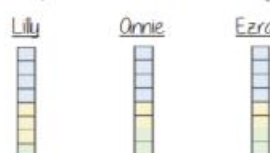
Mean problems

Mean – a measure of average. It gives an idea of the central value

Lily, Annie and Ezra have the following cubes



Finding the mean amount is the average amount each person would have if shared out equally



The mean number of blocks would be 8 each



What do I need to be able to do?

By the end of this unit you should be able to:

- Find a fraction of a given amount
- Use a given fraction to find the whole or other fractions
- Find the percentage of an amount using mental methods
- Find the percentage of a given amount using a calculator

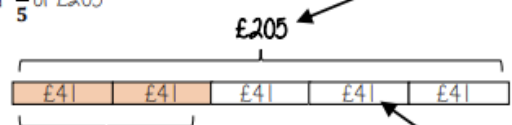
Keywords

- Fraction:** how many parts of a whole we have
- Equivalent:** of equal value
- Whole:** a number with no fractional or decimal part
- Percentage:** parts per 100 (uses the % symbol)
- Place Value:** the value of a digit depending on its place in a number. In our decimal number system, each place is 10 times bigger than the place to its right
- Convert:** change into an equivalent representation, often fraction to decimal to a percentage cycle.

Fraction of a given amount

Find $\frac{2}{5}$ of £205

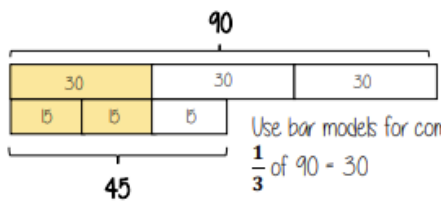
The bar represents the whole amount



2 out of the 5 equal parts
 $2 \times £41 = \underline{£82}$

$£205 \div 5 = £41$

Each part of the bar model represents £41



Use bar models for comparisons

$\frac{1}{3}$ of 90 = 30

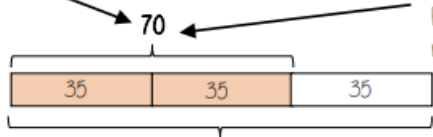
$\frac{2}{3}$ of 45 = 30

$\therefore \frac{1}{3}$ of 90 = $\frac{2}{3}$ of 45

Use a fraction of amount

$\frac{2}{3}$ of a value is 70. What is the whole number?

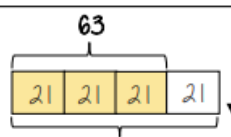
$70 \div 2 = 35$
Each part of the bar model represents 35



$35 \times 3 = 105$
The whole number is 105

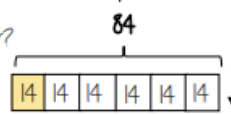
The wording of the question is important to setting up the bar model

$\frac{3}{4}$ of a number is 63.



Find the whole

What is $\frac{1}{6}$ of the number?

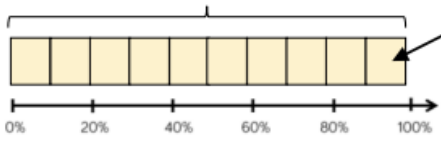


Use the whole to find a given part

-14

Find the percentage of an amount (Mental methods)

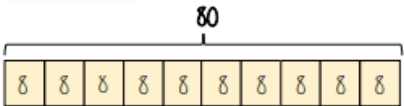
The whole represents 100%



$10\% = \frac{1}{10}$ of the whole

$10\% = \frac{1}{10}$ of the whole $50\% = \frac{5}{10} = \frac{1}{2}$ of the whole
 $20\% = \frac{2}{10} = \frac{1}{5}$ of the whole $5\% = \frac{1}{20}$ of the whole

Find 65% of 80



Method 1
 $65\% = 10\% \times 6 + 5\%$
 $= (8 \times 6) + 4$
 $= 52$

Method 2
 $65\% = 50\% + 10\% + 5\%$
 $= 40 + 8 + 4$
 $= 52$

For bigger percentages it is sometimes easier to take away from 100%

Find the percentage of an amount (Calculator methods)



Using a multiplier

Find 65% of 80

Fraction, decimal, percentage conversion

$65\% = \frac{65}{100} = 0.65$ ← The multiplier

$0.65 \times 80 = 52$

Using the percent button

Find 65% of 80

This brings up the % button on screen
You will see 65%

Type 65

Press **SHIFT** **(%)**

Press **×** 80 and then press **=**

You can also use the calculator to support non calculator methods and find $\frac{1}{10}$ or $\frac{1}{20}$ then add percentages together

"of" can represent 'x' in calculator methods